

A Vivisection of the *ev* Computer Organism: Identifying Sources of Active Information

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Abstract

ev is an evolutionary search algorithm proposed to simulate biological evolution. As such, researchers have claimed that it demonstrates that a blind, unguided search is able to generate new information. However, analysis shows that any non-trivial computer search needs to exploit one or more sources of knowledge to make the search successful. Search algorithms mine active information from these resources, with some search algorithms performing better than others. We illustrate these principles in the analysis of *ev*. The sources of knowledge in *ev* include a Hamming oracle and a perceptron structure that predisposes the search towards its target. The original *ev* uses these resources in an evolutionary algorithm. Although the evolutionary algorithm finds the target, we demonstrate a simple stochastic hill climbing algorithm uses the resources more efficiently.

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INTRODUCTION

Computer algorithms can serve as powerful tools for modeling and studying facets of nature, including biological phenomena. As with all models, extrapolation from algorithm behavior to real-world behavior requires that the algorithm be based on realistic operating assumptions and produce behavior characteristic of the system in question. Inaccuracies or hidden biases can invalidate an algorithm as a model of natural phenomena. Modeling the evolutionary process as an algorithmic search process, therefore, requires diligence on our part to ensure that all algorithm assumptions are realistic and that no undisclosed knowledge sources are used to ease the difficulty of our search.

Algorithms that conduct even moderately sized searches require external assistance to be successful. When such an algorithm produces apparently impressive results, conservation of information [1-3], including the No Free Lunch Theorem [4-11], dictates we are faced with one of two possibilities. The first is that the search problem under consideration is not as difficult as it first appears. At times, the problems solved by seemingly complex algorithms can appear extremely difficult whereas a closer inspection reveals the search is relatively simple and, from a random query or exhaustive search perspective, has a larger probability of success than implicitly supposed. The other alternative, for difficult problems, is that *active information* has been inserted in the search program to increase the chances of success.¹

A common source of active information is a *software oracle*² [12-14]. When the oracle is the dominant computational component in an evolutionary search and the cost of each query is the same, the efficiency of a search algorithm can be measured in query counts. Different search algorithms extract information with varying efficiencies. A simple single agent algorithm that uses a stochastic hill climbing ratchet [13], for example, is much more efficient than an evolutionary search using the oracle available in the artificial life simulation AVIDA [15]. Active information can also be extracted from a *Hamming oracle*.³ The effectiveness of this oracle can range from that of a standard evolutionary search to a deterministic *frequency of occurrence Hamming oracle algorithm*, which can produce over an order of magnitude improvement [13].

This paper presents an analysis of the *ev* program, a search algorithm that models the evolution of nucleotide binding sites [16]. The *ev* algorithm has the form of a perceptron, consisting of a single artificial neuron using a simple threshold nonlinearity. Our purpose is to analyze how *ev*'s search structure constrains performance in light of conservation of information theorems for search algorithms. In particular, we investigate the degree to which *ev*'s success is due to active information introduced into the simulation by the structure of the perceptron used to generate potential solutions and the Hamming oracle used to evaluate the fitness of the solution.

¹ Formally, active information is defined as $-\log_2(p/q)$ where p is the probability of success for an unassisted search and q is the probability of success for an assisted search. Informally, it is the amount of information added to the search that improves the probability of success over the baseline search.

² A software oracle is a software object that answers queries posed to it. In our case, a software oracle is a function that takes in a configuration and returns a value denoting the fitness of that configuration.

³ A Hamming oracle uses the Hamming distance (number of bits that differ from a target sequence) as its fitness metric.

ANALYSIS AND RESULTS

Information measures

We use the following information measures [1,2,13,17,18] to assess the performance of a search:

Endogenous information is a measure of the difficulty of a search and is given by

$$I_{\Omega} = -\log_2 p \quad (1)$$

where p is the probability of success for an unassisted query. *Exogenous information* in a search program is given by

$$I_S := -\log_2 q \quad (2)$$

where q is the probability of success of an assisted query under the same set of constraints.

Active information is the difference between the endogenous and exogenous information, denoted as⁴

$$I_+ := I_{\Omega} - I_S = -\log_2 \frac{p}{q} \quad (3)$$

Each of the three information measures has units of bits. If the knowledge about the space is not accurate or is otherwise misleading, the active information can be negative.

In addition, for any search algorithm, such as **ev**, a resource constraint must be imposed. Otherwise, unlimited time and computer resources would allow an exhaustive search. Let Q denote the query count, Q_{\max} the maximum allowable number of queries before abandoning the search, and E the expectation [19]. Under a query count constraint, the *active information per query*, I_{\oplus} , is

$$I_{\oplus} = E \left[\frac{I_+}{Q} \right] \quad (4)$$

I_{\oplus} can be estimated by averaging the active information per query over K trials of Q_{\max} queries or less. For the k^{th} trial, there are two possibilities. Either success is achieved with $Q_k \leq Q_{\max}$ queries, in which case the point estimate of I_{\oplus} is I_{Ω}/Q_k , or if a success is not achieved with Q_{\max} queries, then the point estimates of I_+ and I_{\oplus} both have a value of zero.

Thus, defining ζ_k such that $\zeta_k = 1$ for a success in Q_{\max} or fewer queries, and $\zeta_k = 0$ and $Q_k = Q_{\max}$ for a failure, we can estimate I_{\oplus} as the average over K trials.⁵ That is, $I_{\oplus} \approx \langle I_{\oplus} \rangle$ where

$$\begin{aligned} \langle I_{\oplus} \rangle &= \frac{1}{K} \sum_{k=1}^K \zeta_k \left(\frac{I_{\Omega}}{Q_k} \right) \\ &= \frac{I_{\Omega}}{K} \sum_{\text{successes}} \frac{1}{Q_k} \end{aligned} \quad (5)$$

This estimate, $\langle I_{\oplus} \rangle$, needs to be interpreted with the same caution as the average speed of an auto on a road trip. Instantaneous values can be significantly higher or lower than the average.

We refer to I_{\oplus}/I_{Ω} as the *normalized active information per query*, and the estimated normalized active information per query is given by

$$\frac{\langle I_{\oplus} \rangle}{I_{\Omega}} = \frac{1}{K} \sum_{\text{successes}} \frac{1}{Q_k} \quad (6)$$

A similar measure⁶ is the *active information per mean query*,

$$I_{\boxplus} = \frac{I_{\Omega}}{E[Q]} \quad (7)$$

which we can estimate by

$$\langle I_{\boxplus} \rangle = \frac{I_{\Omega}}{\langle Q \rangle} \quad (8)$$

where

$$\langle Q \rangle = \frac{1}{K} \sum_{\text{successes}} Q_k \quad (9)$$

Analysis of endogenous information in **ev**

The **ev** search algorithm can be viewed as an *inversion of a perceptron*⁷ [21-23]. This is illustrated in Figure 1 on the next page. The **ev** simulation creates a population of 64 synthetic *organisms*, each with a *genome* consisting of a 256 base string (excluding five extra bases at the end that are not part of the genome proper), with the bases stored as two-bit integers: A=00, C=01, G=10 and T=11. There are, therefore, $n = 256$ nucleotides at the perceptron output that serve as potential binding sites⁸ each with $\Gamma = 4$ possible bases. In this sequence, 16 of the 256 nucleotide site locations are designated as binding sites. The **ev** simulation begins by randomly assigning these 16 binding sites within the second half of the genome and fixes them for the duration of a run. The sequence of ones (binding sites) and zeros (not a binding site) are shown at the bottom of Figure 1. A published example [16] uses the specific locations⁹

$$t = [1, 10, 17, 26, 33, 43, 50, 60, 70, 76, 83, 92, 101, 109, 117, 125]. \quad (10)$$

There is also a $\Gamma \times \lambda$ weight matrix (see Figure 1) with $\Gamma\lambda = 24$ elements that are represented as integers in the range of $[-R, R-1]$ where $R = 512$. Since $2R = 1024 = 4^5$, five bases are needed to give each weight its value. There is a single bias, θ , specified by five bases and having the same range as the weight elements. The perceptron works by sequentially processing the genome in blocks of $\lambda = 6$ bases. As shown in Figure 1, each of the six columns are activated at one of four locations (A, C, G or T) in accordance to the nucleotide above. The weights of these activated locations are summed. The bias, θ , is subtracted from this sum and the result compared to a threshold. If positive, the location is announced as

⁶ From Jensen's inequality [20], $E \left[\frac{1}{Q} \right] \geq \frac{1}{E[Q]}$. Thus $I_{\oplus} \geq I_{\boxplus}$.

⁷ This is a process by which we find a set of weights and bias that give us some desired output behavior for our perceptron.

⁸ Although all 256 positions along the genome are evaluated for errors and contribute to an organism's fitness, the randomly placed binding sites are restricted to the second half of the genome. In Figure 1 of reference 16, these correspond to bases 126 to 261. There are other nucleotides whose identities are interpreted as weights, window values, or the bias in the construction of the perceptron. Five additional bases are used at the end to accommodate a sliding window used in **ev**.

⁹ The target binding sites start at location 131 (zero-indexed) in the first Figure of reference 16. Thus, location 10 here corresponds to nucleotide 141.

⁴ The plus sign subscript on I_+ represents information being added about the search.

⁵ A similar active information rate was used in the dissection of AVIDA [18] using an instruction count rather than queries.

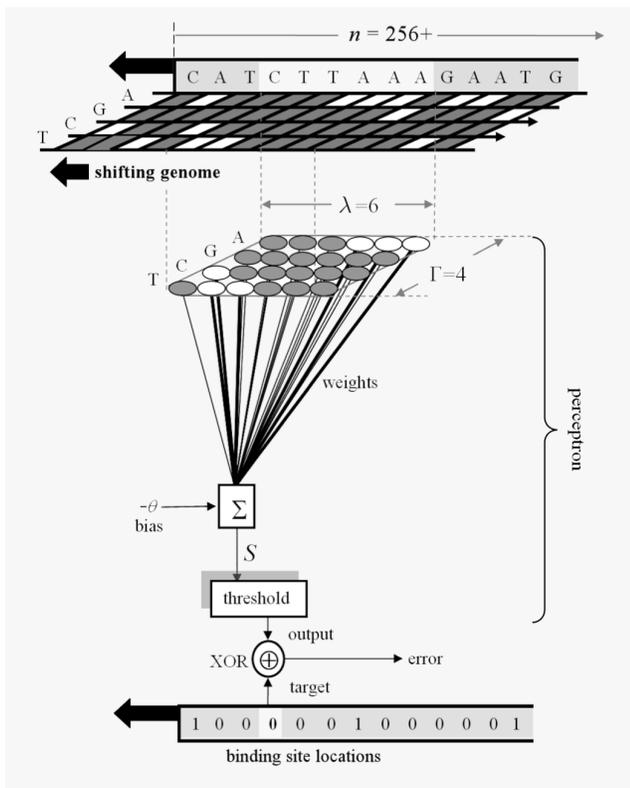


Figure 1. The perceptron structure of *ev*. The genome (top) has at each position $\Gamma = 4$ binary locations, each corresponding to A, G, C and T. The number one is inserted at the location corresponding to the base type, and the number zero is inserted at each of the three remaining locations. These are illustrated with white squares for ones and shaded squares for zeros. The genome's binary locations present binary (0,1)-inputs to the perceptron (middle), illustrated by circles shaded like the squares above them. The strip of the genome is shifted from right to left in unit increments of time. At each point in time, the window of $\lambda = 6$ bases with binary inputs is multiplied by weights, the resulting values are added, and the bias θ is subtracted. The sum S is then compared to the threshold operator. If the final sum is positive, the output is a one; otherwise it is a zero. Finally, the output is compared to the target (bottom). If they are different, an error is tallied. The genome sequence and the target sequence of (0,1)'s is advanced one step, and the process is repeated for the next target bit.

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a binding site. Otherwise, not. This value is compared to the target value. The search problem is to have all of these values match those of the target values, e.g. those in Equation 10. After the complete genome is examined, the total number of places where the perceptron output and the target differs is recorded. This is an exclusive or (XOR) between the two bit strings, and the number of differences between the two is the separating Hamming distance. The Hamming distance tells us how well the perceptron is doing. If the Hamming distance is zero, there is a perfect match and we have found a genome that properly identifies the binding sites.

*Analysis based on *ev* output.* There are at least two ways to analyze the search algorithm in *ev*. The accumulated error from the XOR in Figure 1 is the response to a *Hamming oracle* for a binary alphabet, which announces the total number of bits the target differs from the output. The Hamming oracle is a rich source of active information [13]. Searching only from the perspective of the output, the binary target can be identified with $\langle I_{\oplus} \rangle =$ one bit of active information per query.

A simple approach to demonstrate this is as follows: Query with an output of all ones and record the Hamming distance. Change the first bit to zero. If the Hamming distance is larger, the first bit is a one. If smaller, a zero. Repeat for all the bits. When the second to last bit is identified, the final bit can be identified by matching the Hamming distance measured first. This approach supplies one bit of active information per query. There are other algorithms that extract information from the Hamming oracle more efficiently [13].

*Analysis based on *ev* perceptron structure.* The more interesting case for analysis involves a search using the perceptron structure and the organism's genome, rather than modifying its output directly. In this case, we search for a sequence of nucleotides that produces a weight matrix and bias that calculates a perceptron output identical to the target.

In the search for the binding sites, the target sequences are fixed at the beginning of the search. The weights, bias, and remaining genome sequence are all allowed to vary. Finding them is a form of the perceptron inversion problem [22]. A search space Ω consists of all possible values of weights, genome sequence, and bias. There are 256 nucleotide bases (A, C, G, T) used for each simulation of *ev*. There are 5 additional bases used for a boundary condition for a sliding window across some of the bases. Including these bases, the search space is the 261 fold Cartesian product of the (A, C, G, T) bases. Bases are interpreted in different ways in the search:

1. As a nucleotide on the input strip at the top of Figure 1. There are $256 + \lambda - 1 = 261$ nucleotides in the input strip.
2. As a weight in the $\Gamma \lambda$ matrix. Each weight has 10 bits (5 bases) of precision.
3. As the bias threshold θ . The bias also has 10 bits of accuracy.

Since there are four bases, the cardinality of the search space¹⁰ is

$$|\Omega| = 4^{261} = 1.37 \times 10^{157} \quad (11)$$

Every point in Ω generates an XOR output of 256 bits. The search target Ω_T is the set of all points in Ω that generate the 256 bit target sequence at the output.

Performance analysis of the *ev* perceptron

We now analyze the source the active information provided by *ev*'s perceptron structure. Denote the sum entered into the threshold operator in Figure 1 by S . There are 256 values of S in the output string. Let's call the k^{th} sum S_k and concatenate them into the vector

$$\vec{S} = [S_1 \ S_2 \ S_3 \ \dots \ S_k \ \dots \ S_{256}]^T \quad (12)$$

A given S_k is the sum of seven *independent and identically distributed* (i.i.d.) uniform discrete random variables. The random variables in \vec{S} , though, are not independent. Each, for example, contains the same bias, θ , as one of the seven numbers in its sum. If the output bits were independent, every possible binary string would have the same probability as any other and the same distribution of error. According to the Laplace-DeMoivre theorem [19, 24], they would therefore be Gaussian as in Figure 2B. However, the normalized histogram for *ev* in Figure 2A is far from Gaussian (see below for a demonstration). If the bias is large, it can push

¹⁰ This number includes the five bases that are not searched.

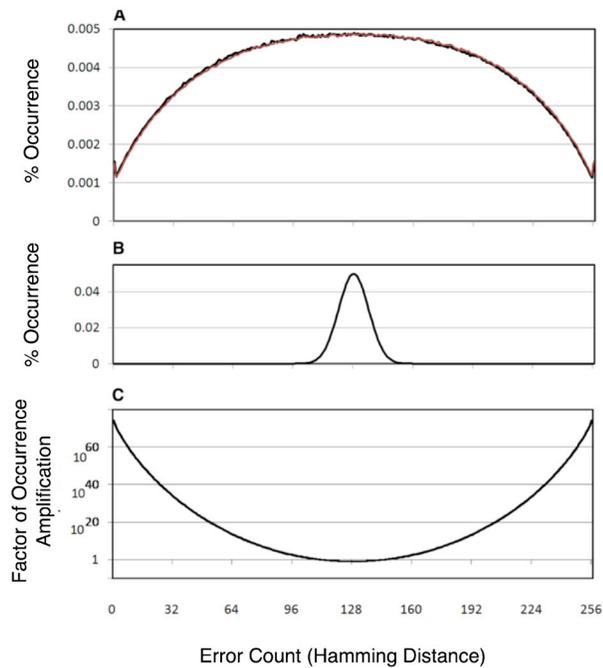


Figure 2. Occurrence frequency of perceptron outputs. **A:** The normalized histogram of the errors in **ev** for ten million trials using an all ones target (red line), and ten million trials using an all zeros target (black line). The two histograms are nearly graphically indistinguishable. There are zero errors in 0.15% of the trials for both. **B:** The Gaussian distribution we expect from the Laplace-DeMoivre theorem. **C:** This curve, equal to the results in A divided by the results in B, reveals the degree to which the frequency of occurrence for output sequences has been amplified by **ev**'s perceptron. The range of all three plots is from zero to 256. The frequency of all zeros expected by a randomly chosen string of bits is multiplied by 1.8×10^{74} by the perceptron. The frequency of occurrences of exactly 16 ones is amplified by a factor of 2.8×10^{49} . [doi:10.5048/BIO-C.2010.3.f2](https://doi.org/10.5048/BIO-C.2010.3.f2)

all of the elements in \vec{S} to be positive. Once the threshold operator is applied, all of the positive values become one. Likewise, the opposite polarity of the bias will push the outputs of the threshold to zero. Only with biases near zero will the resulting binary string be a nearly even mix of ones and zeros. Outcomes with a large number of ones and a few zeros, or few ones and many zeros, are therefore more probable outcomes of the perceptron.

No site a binding site. Analyzing the target sequence consisting of all zeros (*i.e.*, no site is a binding site) illustrates the tendency for the perceptron to produce certain outputs more frequently than others. To see this, we ran the perceptron in Figure 1 once using uniform random sampling with no iteration and assessed the Hamming distance between the perceptron output bits and the target sequence of all zeros. The process was repeated using freshly generated random numbers. Figure 2A shows a histogram of the Hamming distance between randomly generated perceptron outputs and the target sequence for ten million such trials when the target sequence is all zeros. Rather than dipping to nearly zero at the origin, the *empirical probability of success* is

$$q = 0.00155. \quad (13)$$

The exogenous information for an output of all zeros is therefore only $I_s = \log_2(q) \approx 9$ bits.¹¹ Similar experiments were per-

¹¹ From Jensen's inequality [20], $E[\log_2 p] \leq \log_2 E[p]$, so this estimate is biased. The probability of predicting the outcome of 9.3 flips of a fair coin, however, is given by Equation 13. The same comment applies for Equations 15 and 16.

formed for an all ones target sequence, with nearly identical results.¹² The substantial decrease in difficulty (9 bits instead of the expected 256 bits) is due to active information introduced by the perceptron structure for an all zeros target. The reason, as we have shown, is that the **ev** perceptron is heavily predisposed for generating successful solutions for targets of the type shown in Equation 10 where a few ones are sprinkled in a sea of zeros.

A total of 261 nucleotides defines the perceptron structure in Figure 1, and the size of the search space is given by Equation 11. It follows that an astounding $q|\Omega| \approx 2 \times 10^{154}$ genome sequences produce an output of all zeros.

An upper bound on exogenous information. Despite this predisposition, the probability of an unassisted search generating zeros with sparsely occurring ones, as specified for example in Equation 10, is still very small. We have two empirical estimates of the upper bound on the endogenous information of the **ev** problem. In both cases we conservatively assume there is only one perceptron that generates an output matching a desired 16 bit target, like that of Equation 10.

First, from the data used to plot Figure 2A, the frequency of occurrence of strings with zeros with precisely 16 ones is 0.0024. The probability of hitting the target in Equation 10 is then $p = \Pr[\text{hitting target}] = \Pr[\text{hitting target} | 16 \text{ ones}] \times \Pr[16 \text{ ones}]$. There are

$$\frac{1}{\pi} = \binom{256}{16} \approx 10^{25} \quad (14)$$

possible ways to arrange 16 ones and 240 zeros. Because there have been successful simulations, we know at least one of these can match the target sequence. Thus $\Pr[\text{hitting target} | 16 \text{ ones}] \geq \pi$ and $p \geq 0.0024 \times \pi = 2 \times 10^{-28}$. We can therefore estimate

$$I_s < 92 \text{ bits.} \quad (15)$$

Second, **ev** requires that all binding sites be restricted to the second half of the genome (positions 126 through 256), as they are in the target sequences. After randomly initializing 1.5 billion independent genomes, 187 outputs were found to have exactly 16 ones occurring along the second half of the genome. Repeating the above calculations¹³ results in the slightly tighter bound of

$$I_s < 90 \text{ bits.} \quad (16)$$

Search algorithms using the **ev** perceptron.

A search algorithm's role is to extract active information from the knowledge sources. Some search procedures do this better than others. In the case of **ev**, sources of knowledge guiding the search include the Hamming oracle and the predisposition of the perceptron to generate outputs that favor the type of targets shown. We show here that the evolutionary algorithm originally used for **ev** performs worse than simple stochastic hill climbing.¹⁴

Algorithm A1 (stochastic hill climbing). Stochastic hill climbing can be performed at the perceptron level involving all of the

¹² We found 15,234 successes in 10 million trials. For a target sequence of all ones, therefore, $p = 0.00152$.

¹³ We recalculated using $\binom{131}{16}$ to reflect the smaller number of potential binding site positions.

¹⁴ This is also the case for AVIDA software [15]. The evolutionary search algorithm used in the original paper was shown to extract information from the knowledge sources in the program much less efficiently than other search algorithms [18].

genome bases in **ev**. We initialized by choosing 261 genome bases at random, and then computed the error output (see Figure 1). One of the 261 bases was replaced at random and the error output was recomputed. If the error was the same or smaller, the change was kept. If not, the change was discarded and the process repeated.¹⁵ Simulation of $K = 10,000$ separate searches¹⁶ with $Q_{\max} = 100,000$ and random initializations produced a 100% success rate. The average number of queries for success was $\langle Q \rangle = 10,601$. According to Equation 8, the estimated normalized active information per mean query for algorithm *A1* is therefore

$$\frac{\langle I_{\boxplus} \rangle}{I_{\Omega}} \approx 1.09 \times 10^{-4} \quad (17)$$

Algorithm A2 (evolutionary perceptron inversion of ev). The original **ev** program [16] used an evolutionary search algorithm for finding binding sites. The search was seeded with $M = 64$ randomly selected *organisms* and, in each iteration, two adjacent bits from a randomly chosen nucleotide in each organism were discarded, replacing them with two randomly chosen bits. (As before, the nucleotides are represented by two-bits.) Half of the mutated genomes with the highest fitness were then selected to be the parents of the next generation.¹⁷

Using $Q_{\max} = 100,000$ as the maximum query count per search¹⁸, simulation of $K = 10,000$ separate searches using randomly generated initializations produced 9,115 successes. The average number of queries for success was, $\langle Q \rangle = 63,568$ or 993 *generations*. This compares to the single simulation result of 704 generations reported in the original **ev** paper [16]. Applying Equation 6, the estimated normalized active information per mean query for algorithm *A2* thus gives

$$\frac{\langle I_{\boxplus} \rangle}{I_{\Omega}} \approx 1.55 \times 10^{-7} \quad (18)$$

Comparing with Equation 17, we see that algorithm *A1* is roughly 700 times more efficient than *A2*, the evolutionary algorithm used by **ev**.

The effect of differing mutation rates. The above results were obtained using a fixed mutation rate of one base change (two bits) per organism per generation for both *A1* and *A2*. We further measured the search performance of the *A2* strategy using several different mutation rates¹⁹. A comparison of success rate and mutation rate for the *A2* algorithm is shown in Figure 3. The optimal mutation rate for *A2* was found to be roughly 1.75 mutations per child,²⁰ per generation, with the 1 mutation per child rate chosen by Schneider being slightly less efficient, but still within the range of workable mutation rates.

The effect of random uniform generated binding sites in stochastic hill climbing. We have shown the perceptron favors gen-

eration of strings of output zeros peppered with occasional ones, or ones peppered with zeros. The target sequences generated in the original **ev** program are the former. Further experiments demonstrated a severe performance decrease when the binding sites are chosen by a 50-50 coin flip. We simulated the **ev** search using randomly generated binding sites with each site along the second half of the genome (positions 126 through 256) having a 50% chance of being marked as a binding site. We measured the performance using mutation rates of 1, 1.5, 2, 4 and 8 mutations per child, per generation, with a query cutoff of $Q_{\max} = 100,000$ queries for 10,000 runs each. The **ev** search was only successful for mutation rates of 1 and 1.5, failing to find the target in under 100,000 queries for all other mutation rates. A mutation rate of 1 mutation per child using the random 50-50 bindings resulted in a success rate of only 0.05 (compared to the prior success rate of 0.91), while a mutation rate of 1.5 mutations per child resulted in a success rate of 0.0003 (compared to the prior success rate of 0.99). Changing the binding sites pattern to an even mix of zeros and ones therefore severely hampers search performance.

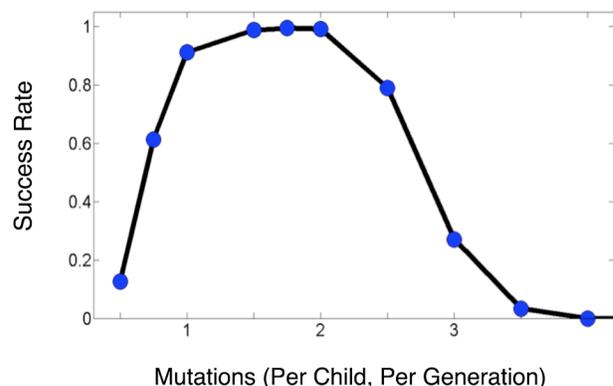


Figure 3. Search success rate vs. mutation rate for algorithm A2. Results are from a population size of 64 and a query cutoff of $Q_{\max} = 100,000$ queries. doi:10.5048/BIO-C.2010.3.f3

CONCLUSIONS

The success of **ev** is largely due to active information introduced by the Hamming oracle and from the perceptron structure. It is not due to the evolutionary algorithm used to perform the search. Indeed, other algorithms are shown to mine active information more efficiently from the knowledge sources provided by **ev** [13].

Schneider [16] claims that **ev** demonstrates that naturally occurring genetic systems gain information by evolutionary processes and that “information gain can occur by punctuated equilibrium”. Our results show that, contrary to these claims, **ev** does not demonstrate “that biological information...can rapidly appear in genetic control systems subjected to replication, mutation, and selection” [16]. We show this by demonstrating that there are at least five sources of active information in **ev**.²¹

1. *The perceptron structure*. The perceptron structure is predisposed to generating strings of ones sprinkled by zeros or strings of zeros sprinkled by ones. Since the binding site target is mostly zeros with a few ones, there is a greater

²¹ Two of the sources of active information, 3 and 4, are discussed in our previous work [1,2,5].

¹⁵ This algorithm is commonly denoted as (1+1)-ES [25,26].

¹⁶ All experimental results in this paper were obtained using the online **ev** simulation software available at <http://www.evoinfo.org/ev>.

¹⁷ The standard notation for this algorithm is (32,64)-ES [25,26].

¹⁸ 10,000 populations each running for a maximum of 1,563 generations (corresponding to $Q_{\max} = 64 \times 1,563 \approx 100,000$ queries).

¹⁹ All tests were performed with 10,000 runs, using a population size of 64 and a query cutoff of 100,000 queries.

²⁰ Fractional mutations are generated by randomizing the mutation number. To achieve 1.75 mutations per child, each child receives at least one mutation and has a 75% chance of receiving an additional, second mutation.

predisposition to generate the target than if it were, for example, a set of ones and zeros produced by the flipping of a fair coin.

2. *The Hamming Oracle* [13]. When some offspring are correctly announced as more fit than others [27], external knowledge is being applied to the search and active information is introduced. As with the child's game, we are being told with respect to the solution whether we are getting "colder" or "warmer".
3. *Repeated Queries*. Two queries contain more information than one. Repeated queries can contribute active information [1,2,5].
4. *Optimization by Mutation*. This process discards mutations with low fitness and propagates those with high fitness. When the mutation rate is small, this process resembles a simple Markov birth process [27] that converges to the target [1,2,5].
5. *Degree of Mutation*. As seen in Figure 3, the degree of mutation for **ev** must be tuned to a band of workable values.

Our analysis highlights the importance of disclosing sources of knowledge in computer searches when measuring the ability of search mechanisms to generate novel information. As far as **ev** can be viewed as a model for biological processes in nature, it provides little evidence for the ability of a Darwinian search to generate new information. Rather, it demonstrates that preexisting sources of information can be re-used and exploited, with varying degrees of efficiency, by a suitably designed search process, biased computation structure, and tuned parameter set. This confirms that the conservation of information principle, as manifest in the No Free Lunch Theorems, is "very useful, especially in light of some of the sometimes-outrageous claims that had been made of specific optimization algorithms" [4].

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